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Author(s): Xiaoyu Alan Zheng, Johannes Soons

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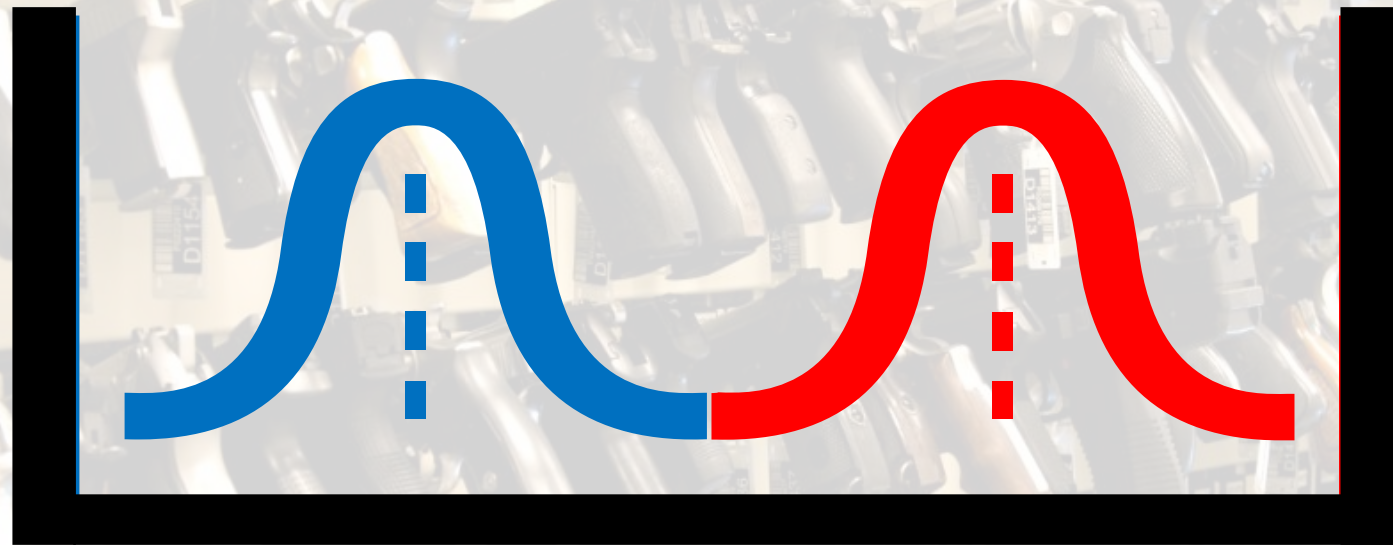
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Population Statistics for Firearm Toolmark Analysis



Xiaoyu Alan Zheng, Johannes Soons
National Institute of Standards and Technology

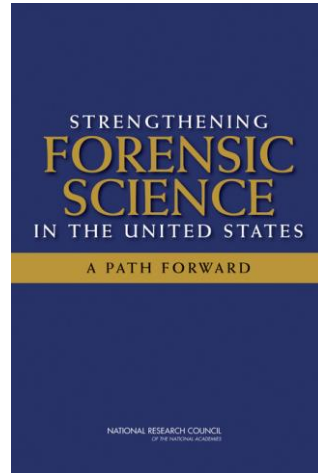
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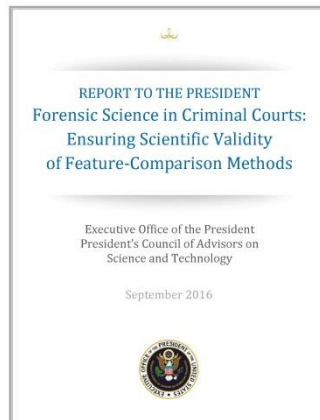
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Motivation



- NAS 2009 “..the decision of the toolmark examiner remains a **subjective decision** based on unarticulated standards and no statistical foundation for **estimation of error rates.**”

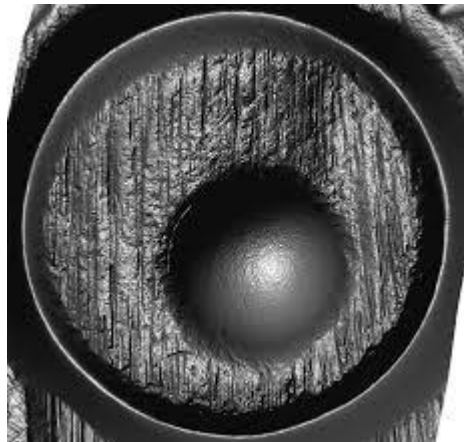
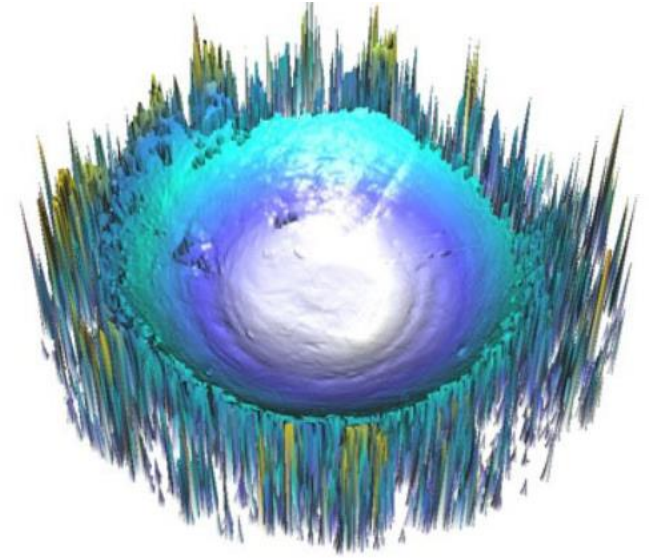
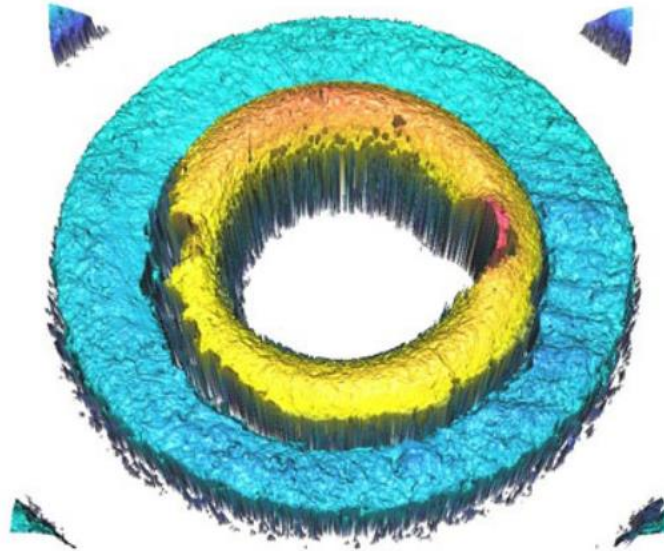


- PCAST 2016: “PCAST finds that firearms analysis currently falls short of the criteria for foundational validity, because there is only a single appropriately designed study to **measure validity and estimate reliability.**”

“If firearms analysis is allowed in court, the scientific criteria for validity as applied should be understood to require **clearly reporting the error rates seen in appropriately designed black-box studies.**”

“A second – and more important – direction is ... to convert firearms analysis **from a subjective method to an objective method...**”

3D Measurements



Bullet Land Engraved Area

Documentary Standards



- Standard for Toolmark Topography Comparison Software
- Standard for Implementation of 3D Technologies in Forensic Laboratories
- Standard for 3D Measurement Systems and Measurement Quality Control



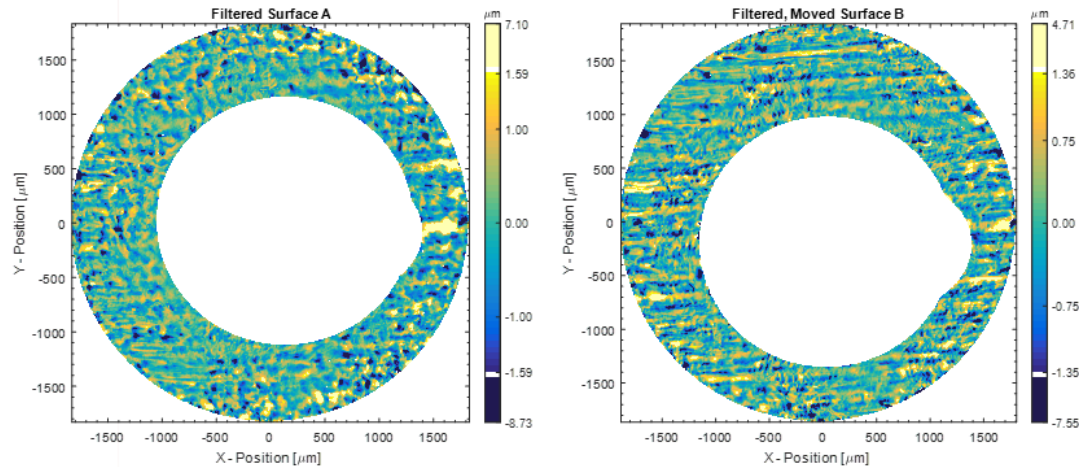
- Best Practice guides for Quality Assurance of 3D instruments that are used for VCM.
- Procedure for Conducting a Virtual Comparison Microscopy (VCM) Deployment Validation for Firearms and Toolmarks



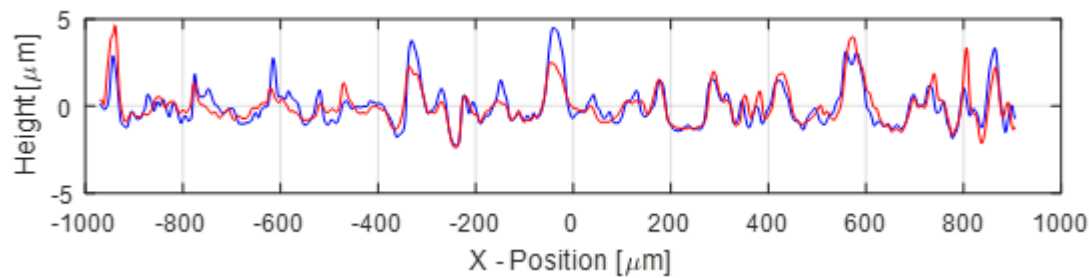
- Unambiguous file exchange standard
- Open-FMC.org
- ISO25178-72 XML 3D Profile

Algorithms

Area Based Correlation

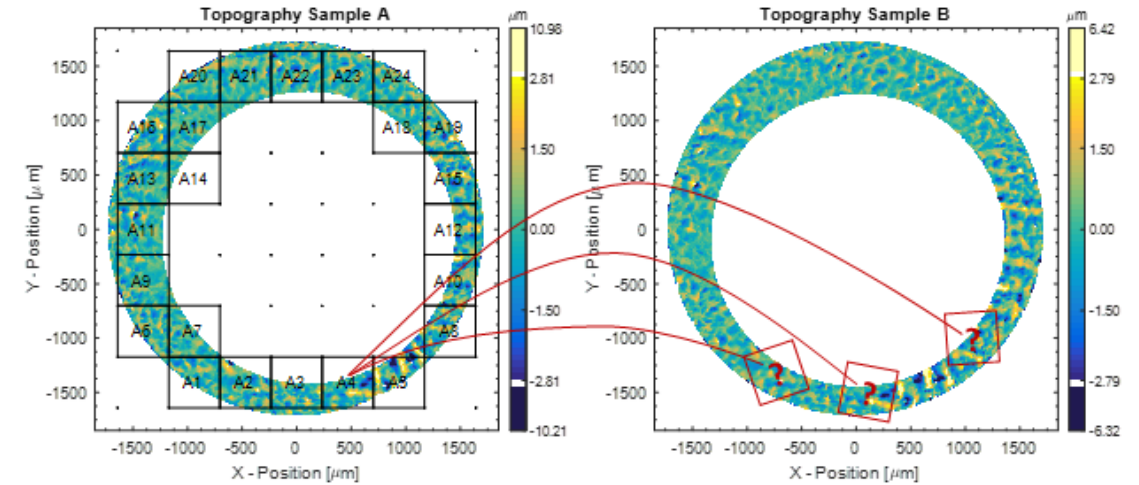


Areal Cross Correlation Function ($ACCF_{MAX}$)

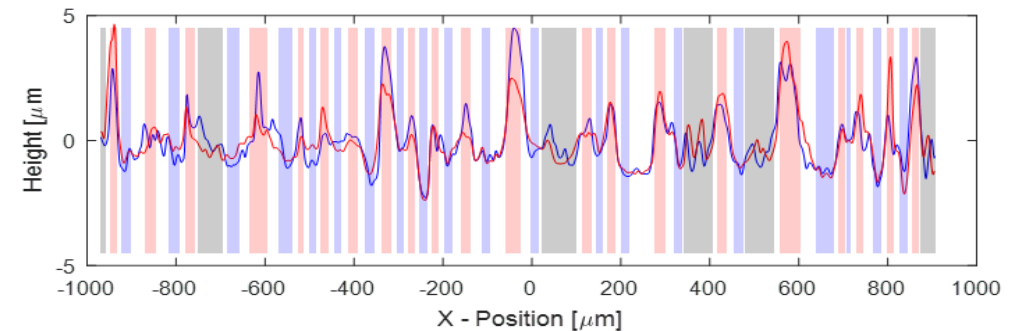


Cross Correlation Function (CCF_{MAX})

Feature Based Correlation



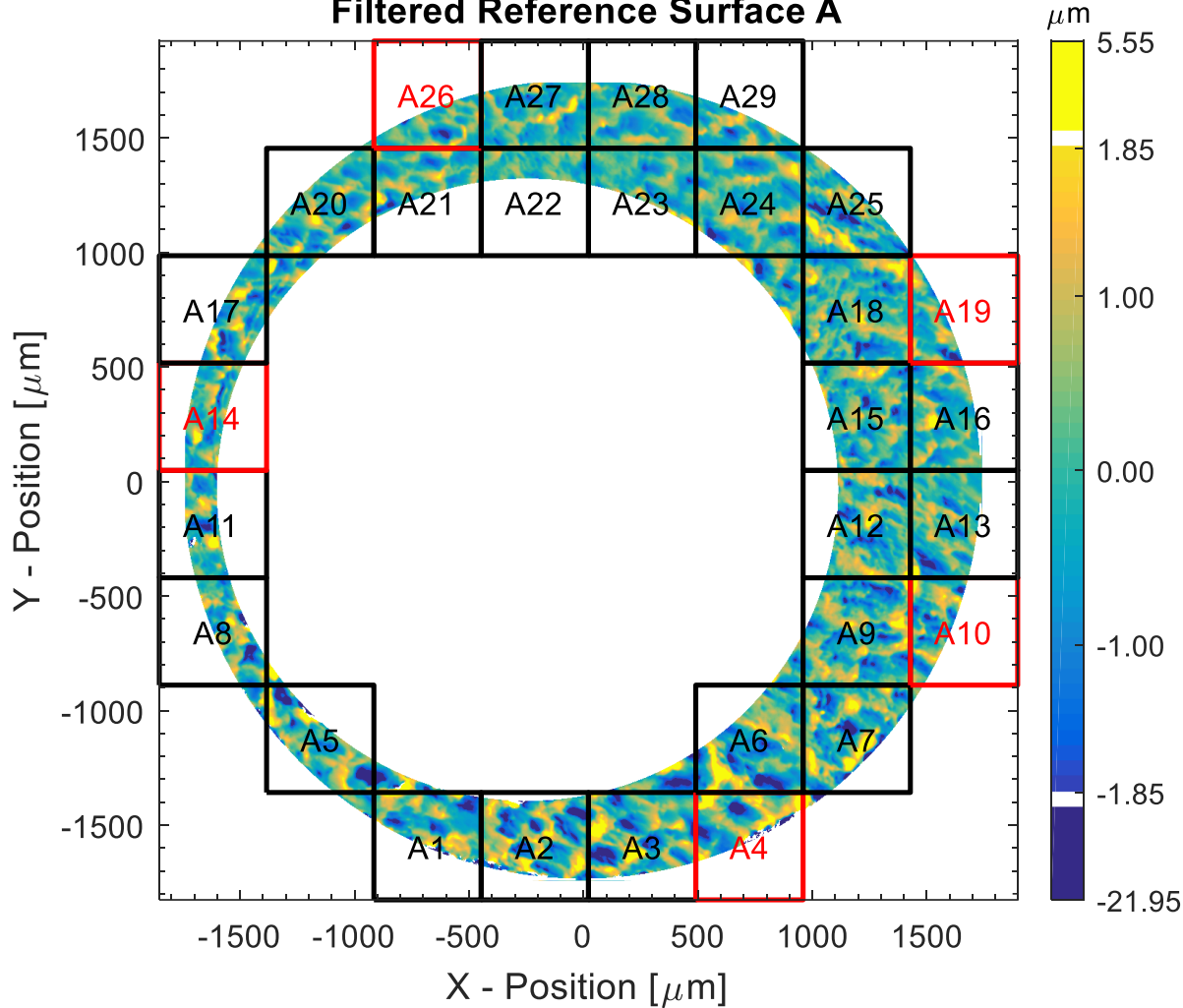
Congruent Matching Cells (CMC)



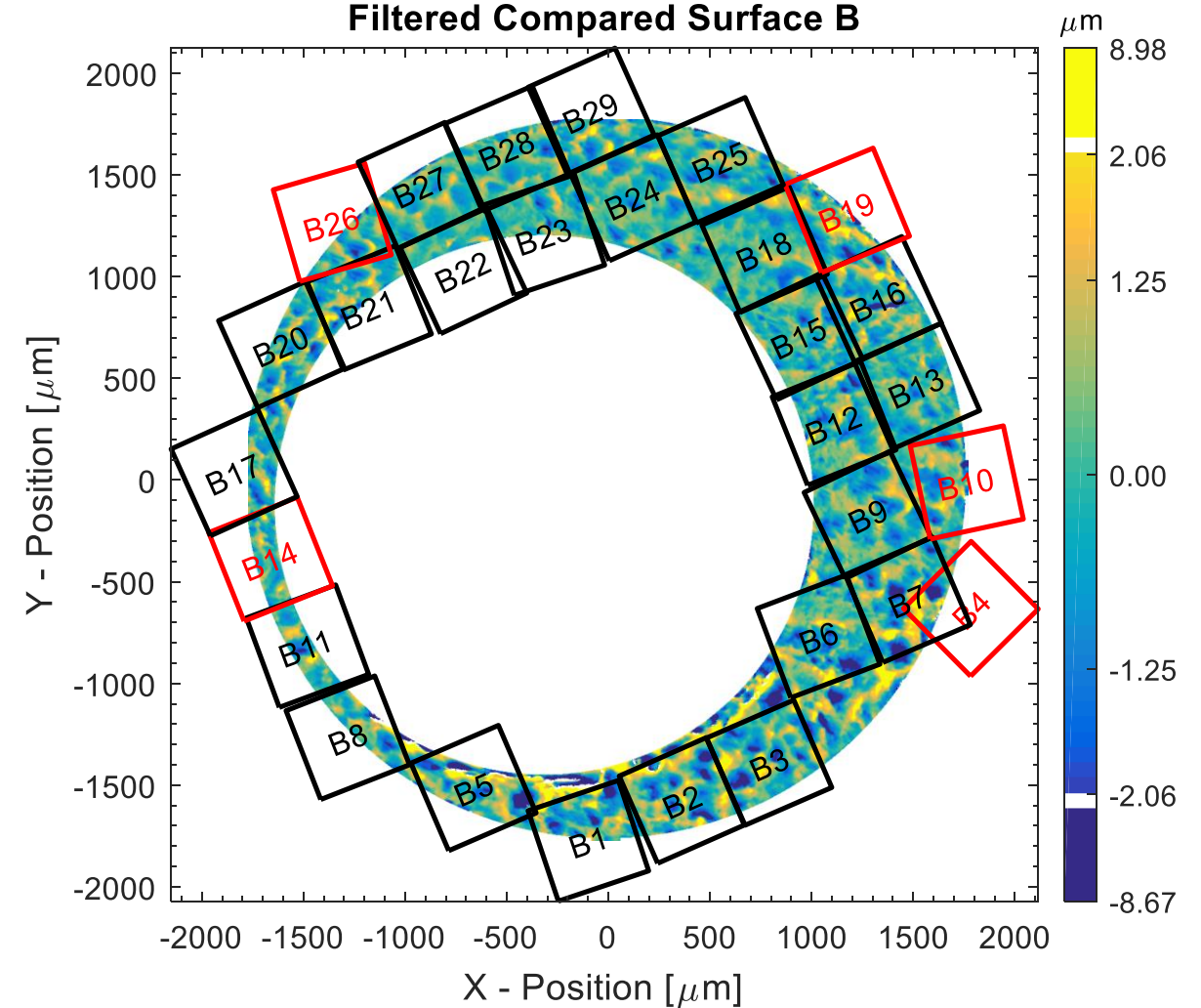
Consecutive Matching Striae (CMS)

CMC Algorithm – KM

Filtered Reference Surface A

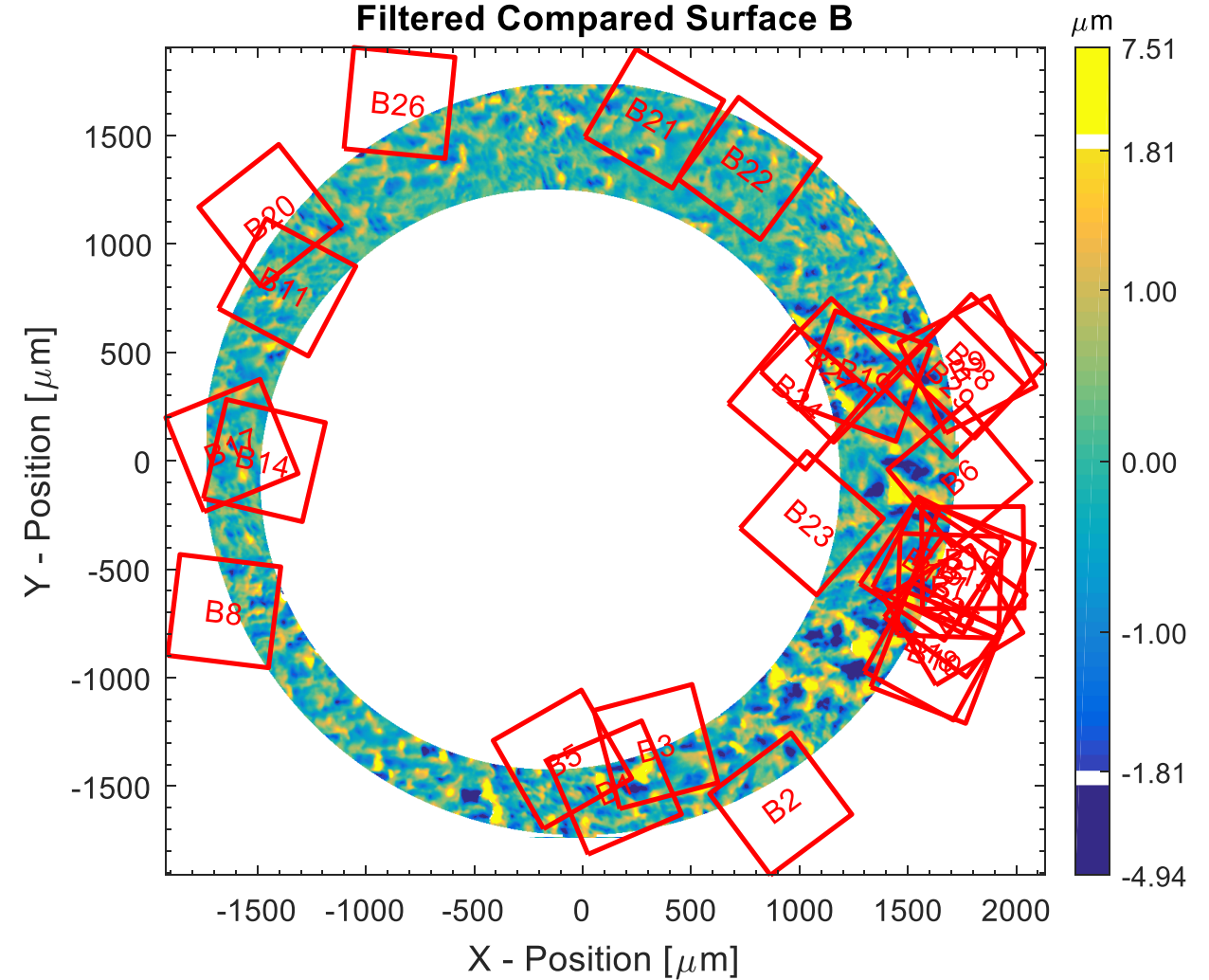
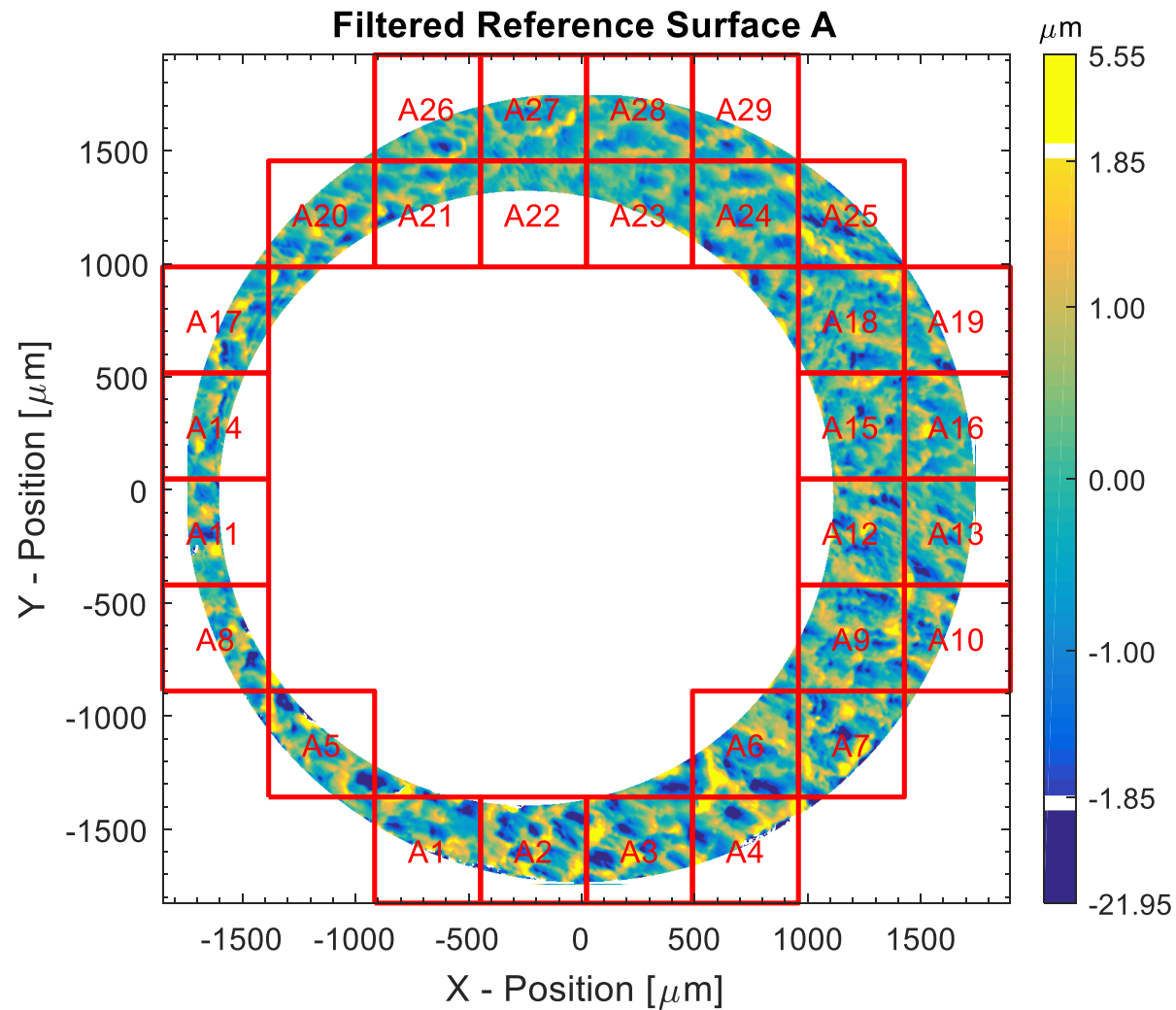


Filtered Compared Surface B



24 CMCs

CMC Algorithm - KNM



0 CMCs

Firearm Brand and Ammo



104 Firearms



100 Firearms



115 Gr FMJ

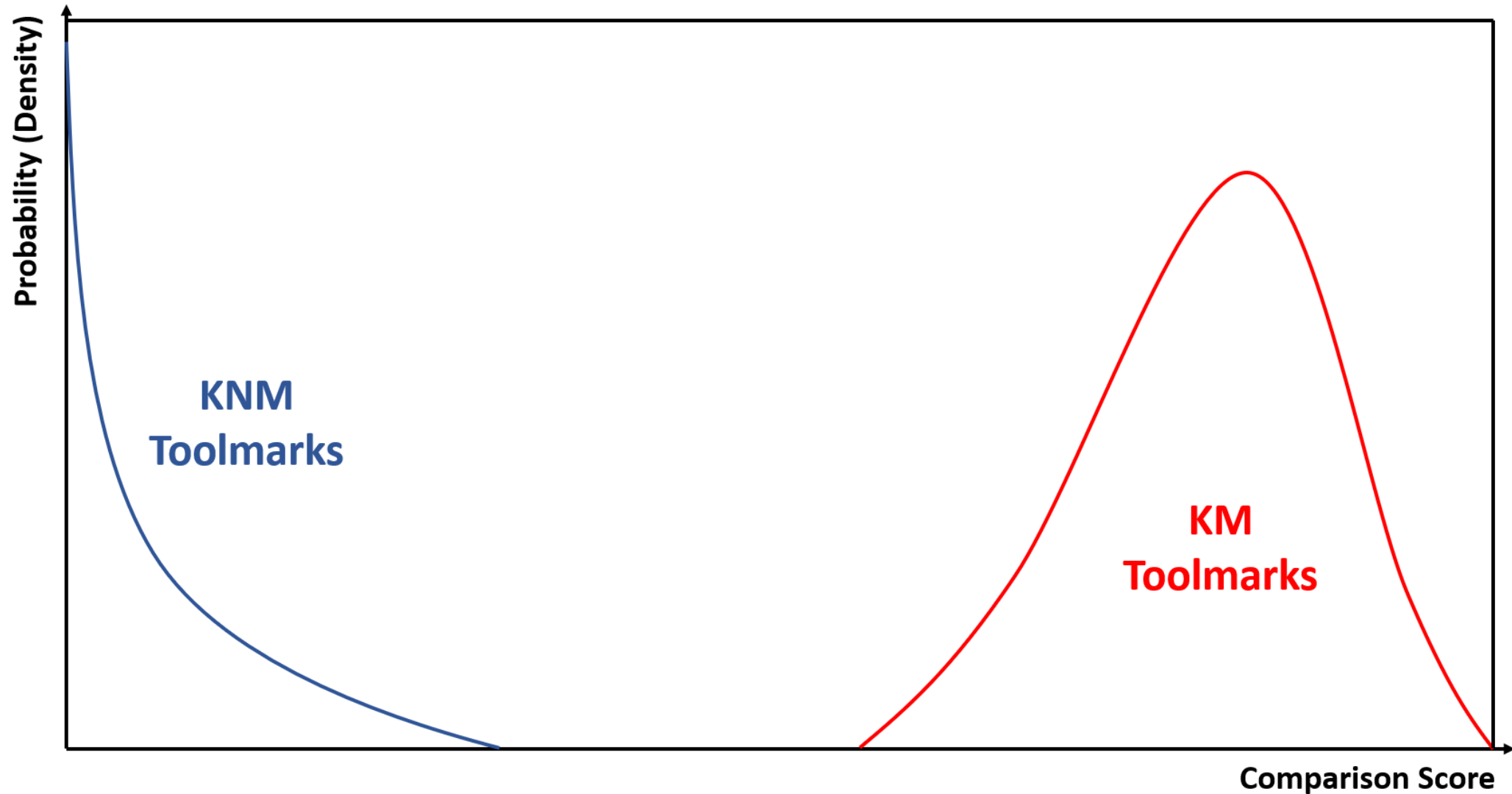


115 Firearms

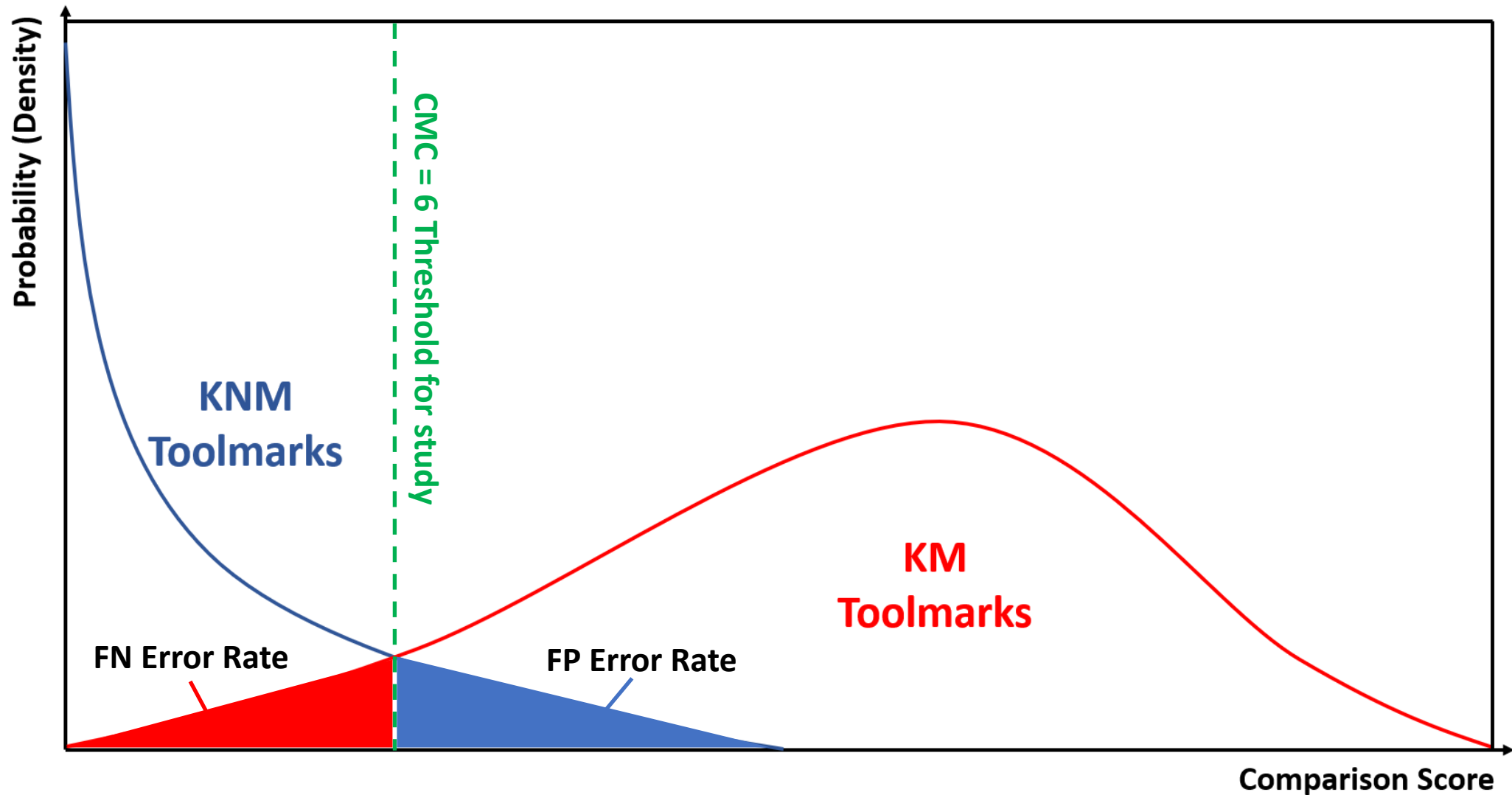


91 Firearms

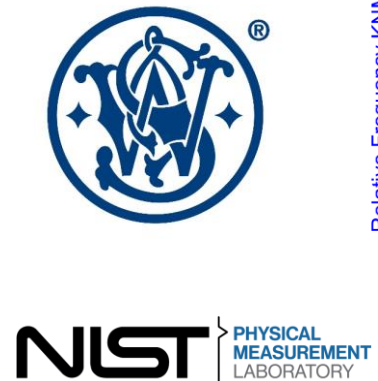
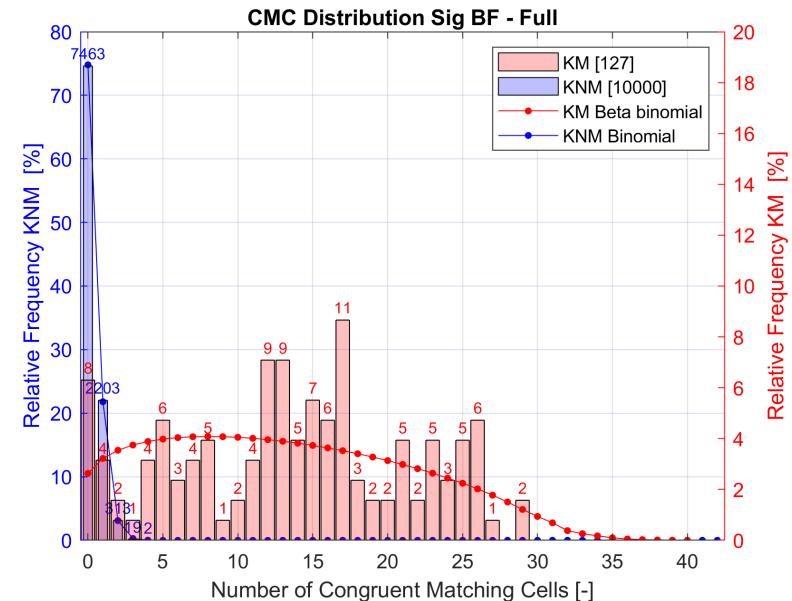
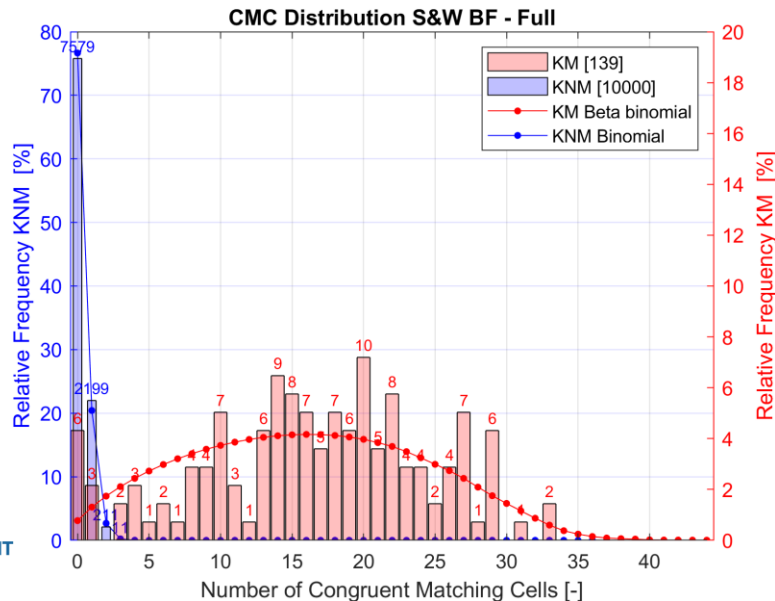
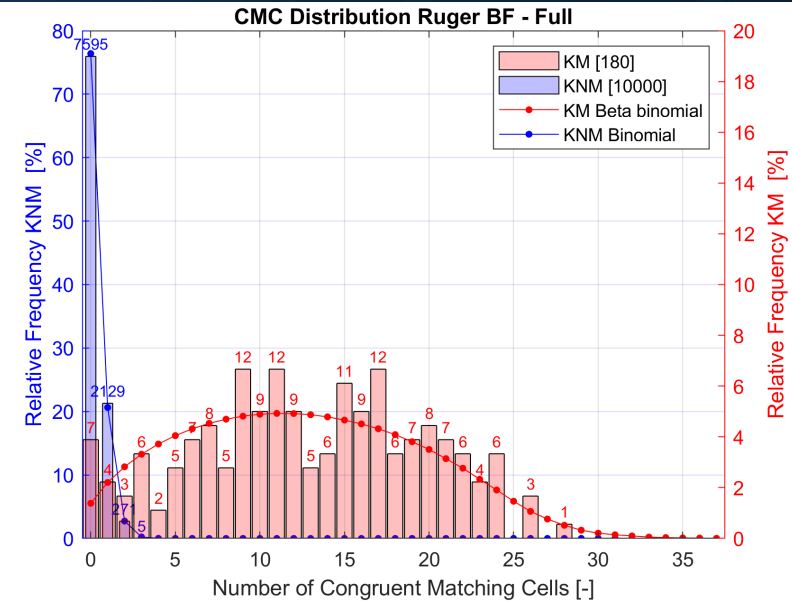
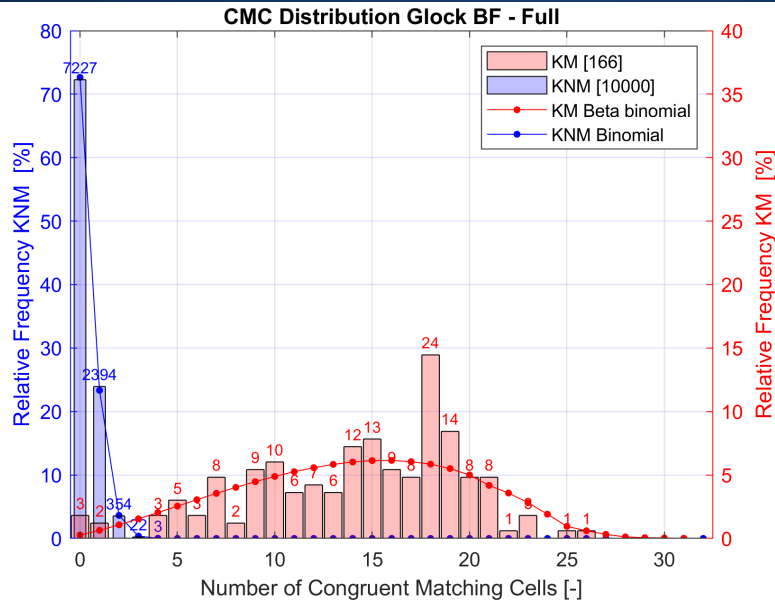
Perfect World



System Error Rates

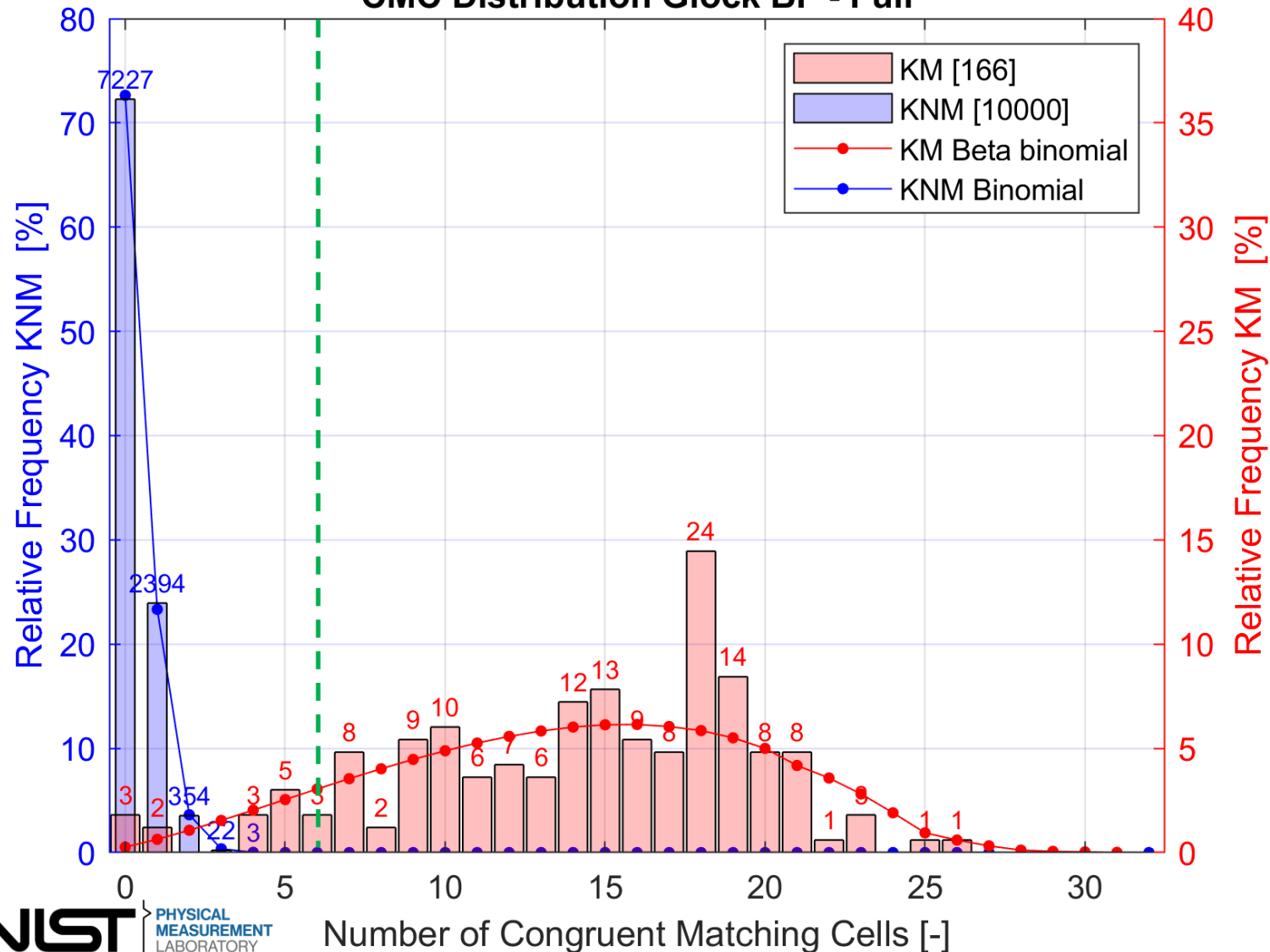


Full BF Populations



Glock – Full Population

CMC Distribution Glock BF - Full



Cumulative False Positive Probability:

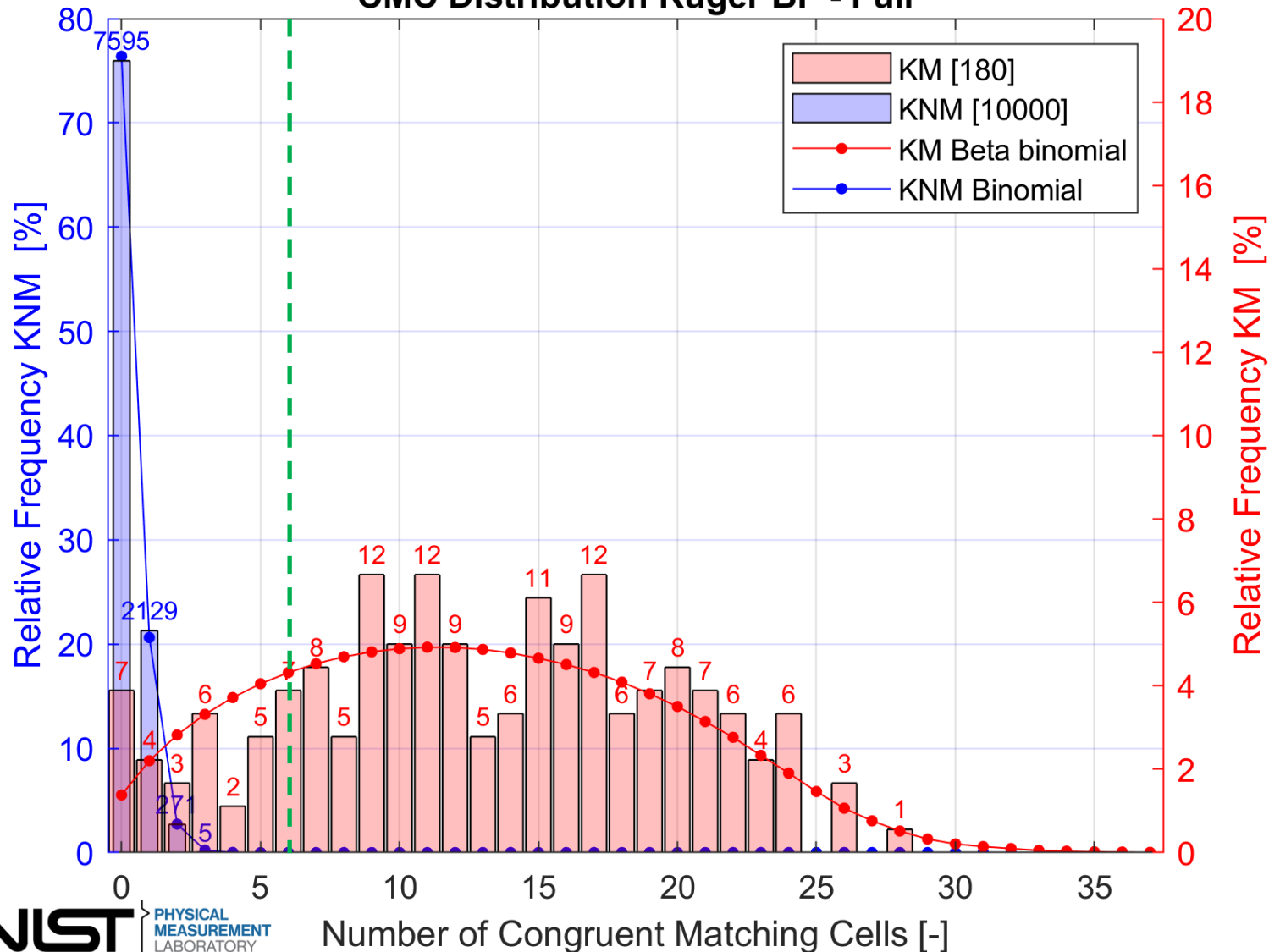
0.000071 %

Cumulative False Negative Probability:

8.10 %

Ruger – Full Population

CMC Distribution Ruger BF - Full



Cumulative False Positive Probability:

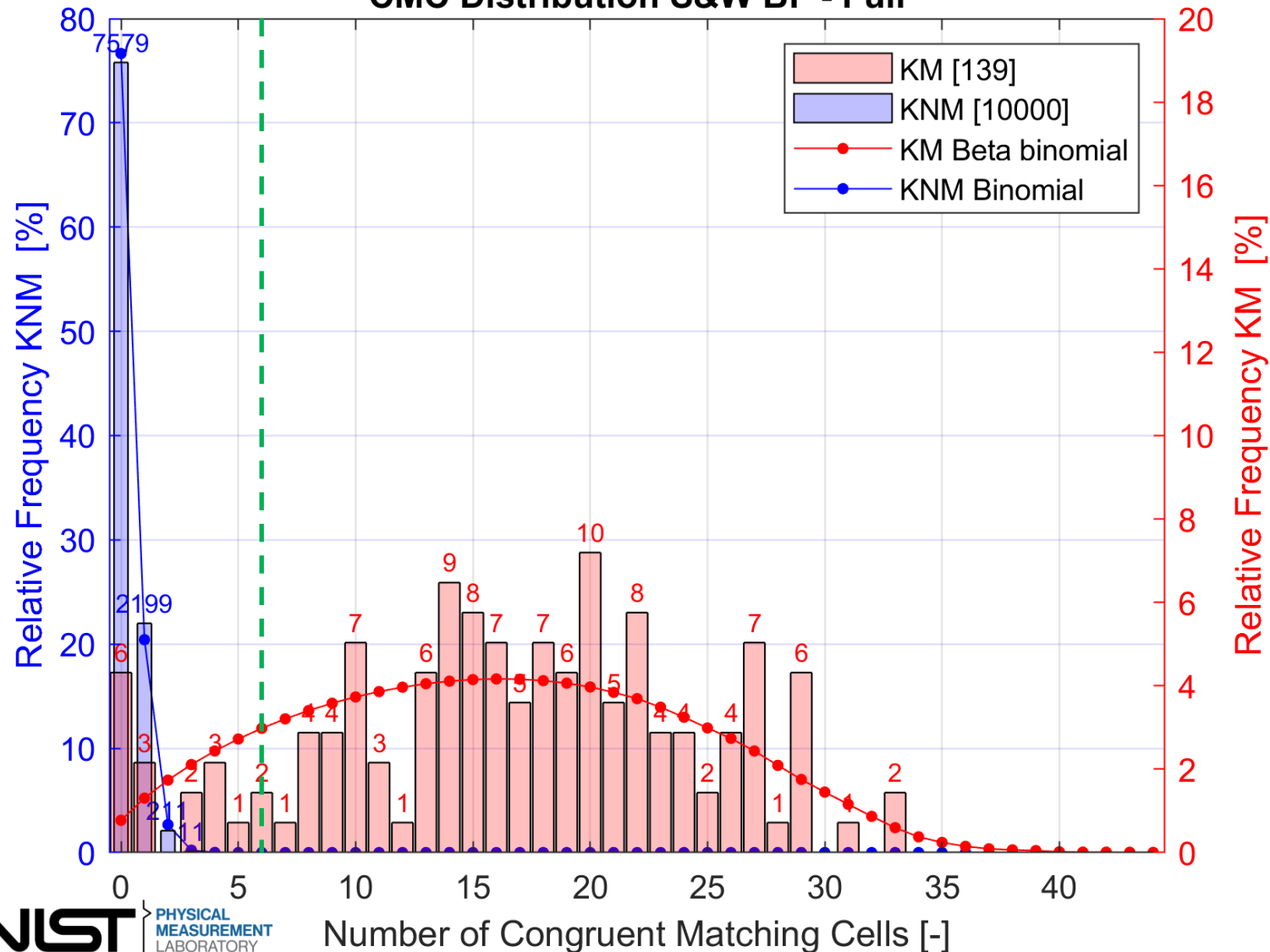
0.000031 %

Cumulative False Negative Probability:

17.49 %

S&W – Full Population

CMC Distribution S&W BF - Full



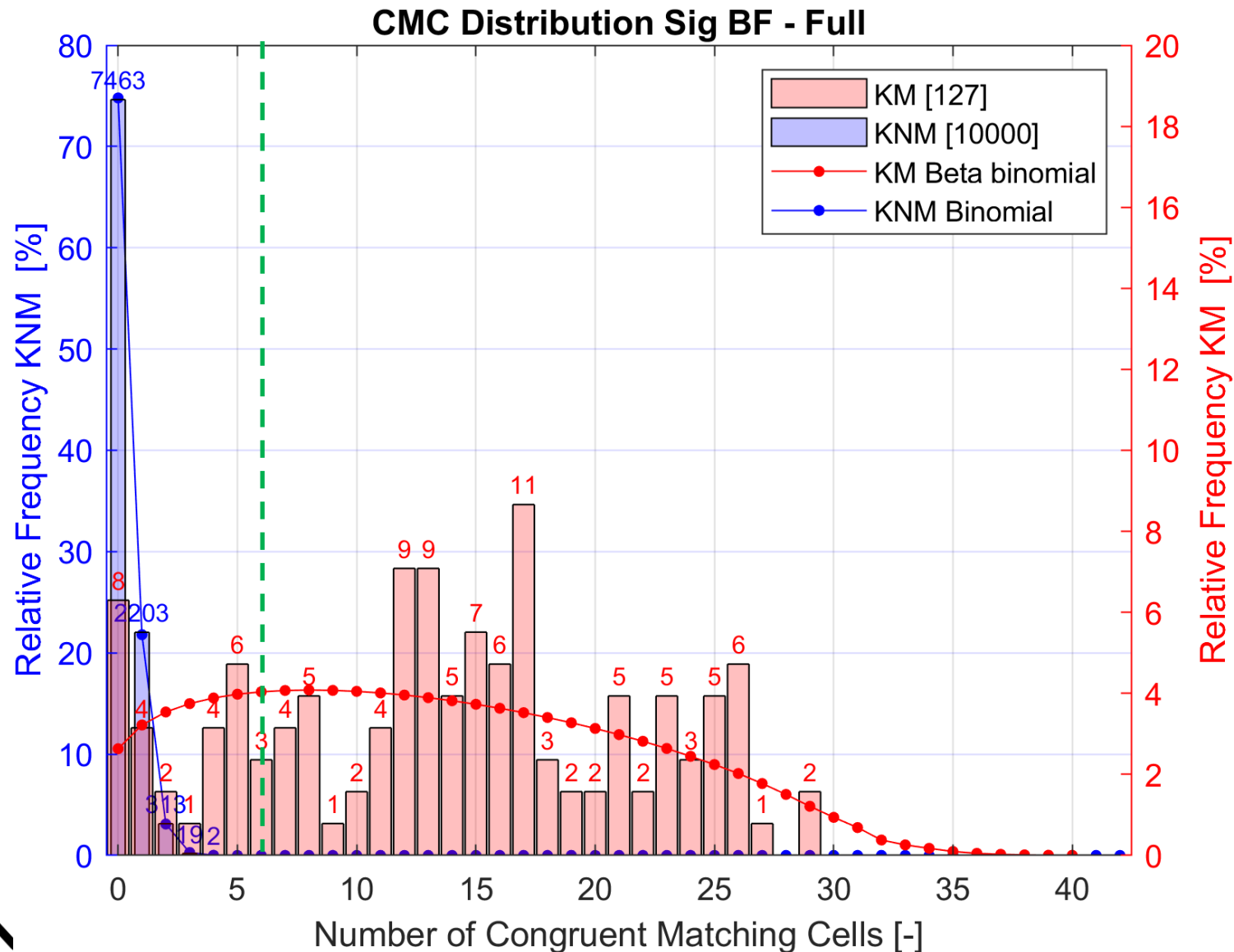
Cumulative False Positive Probability:

0.000031 %

Cumulative False Negative Probability:

11.09 %

Sig – Full Population



Cumulative False Positive Probability:

0.000046 %

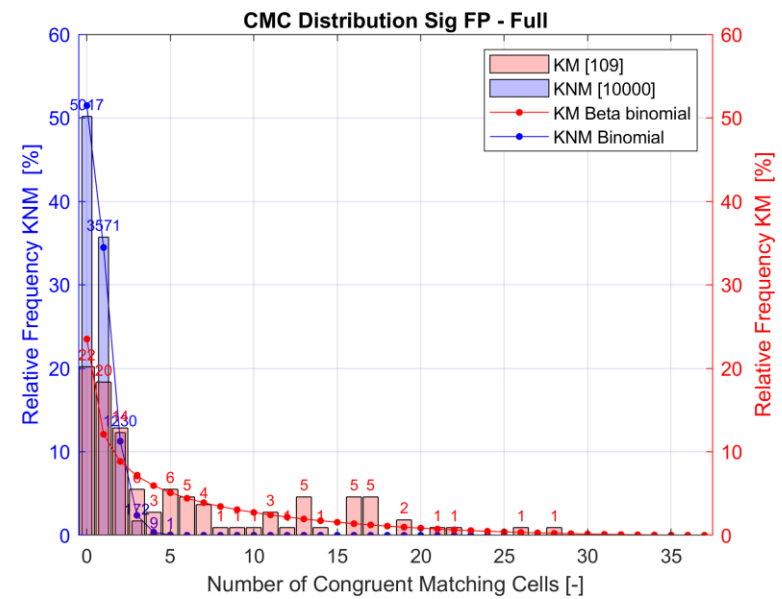
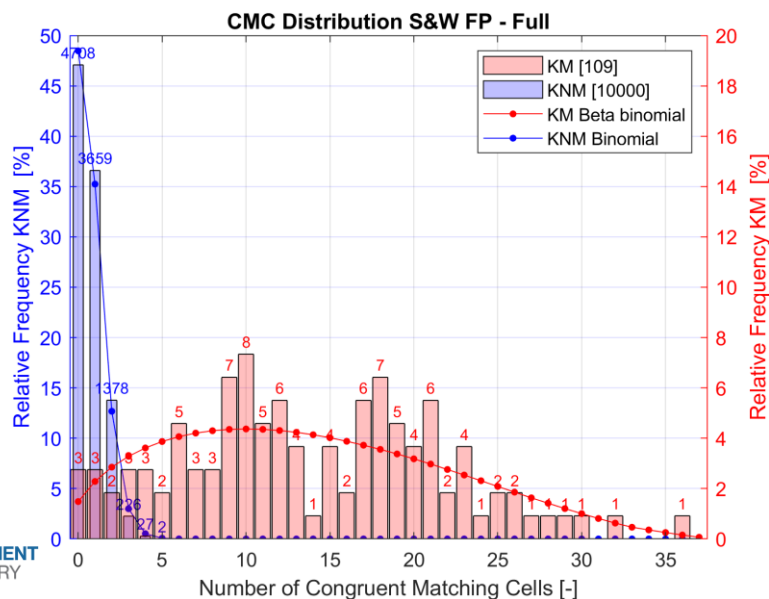
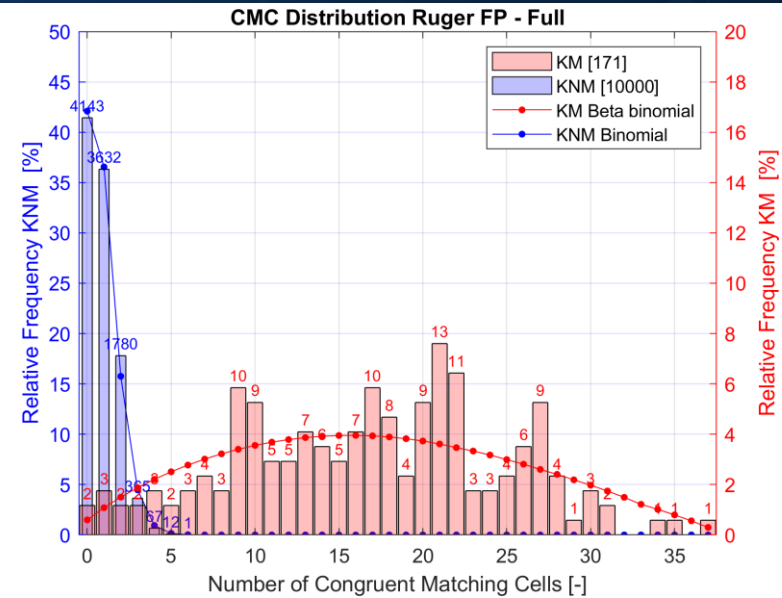
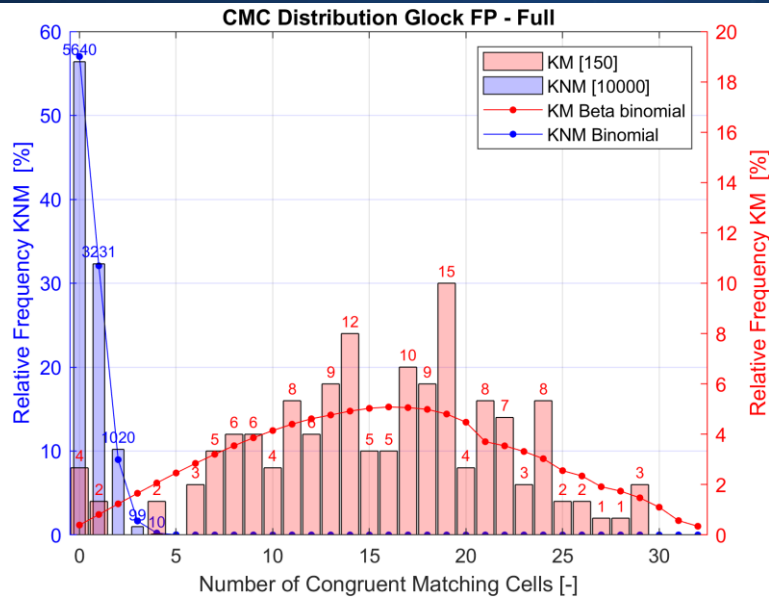
Cumulative False Negative Probability:

21.01 %

BF Data Summary

Population	Cumulative False Positive Error Rate	Cumulative False Negative Error Rate
Glock Full	0.000071 %	8.10 %
Glock Granular	0.000049%	8.68 %
Glock Parallel	0.00021 %	6.39 %
Ruger Full	0.000031 %	17.49 %
Ruger Granular	0.000023 %	18.17 %
Ruger Parallel	0.000055 %	16.77 %
S&W Full	0.000031 %	11.09 %
S&W Granular	0.000019 %	18.86 %
S&W Parallel	0.000075 %	1.62 %
Sig Full	0.000046 %	21.01 %
Sig Granular	0.000014 %	26.50 %
Sig Parallel	0.00027 %	15.24 %

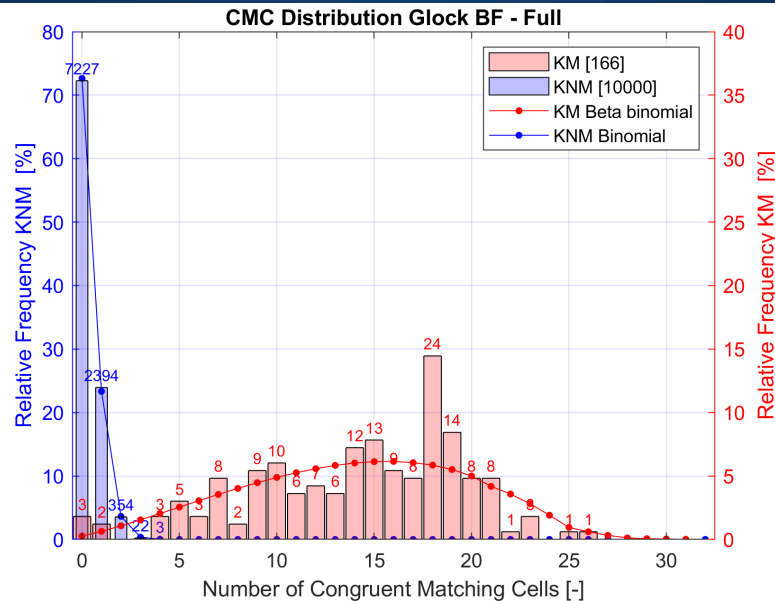
Full FP Populations



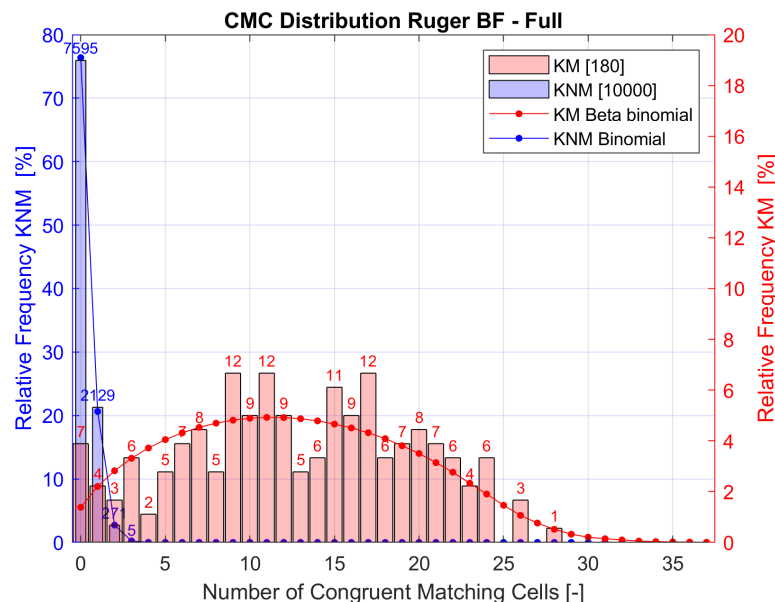
FP Data Summary

Population	Cumulative False Positive Error Rate	Cumulative False Negative Error Rate
Glock Full	0.0025 %	8.62 %
Ruger Full	0.024 %	9.78 %
S&W Full	0.0088 %	17.39 %
Sig Full	0.0047 %	62.59 %

1 in 10 Million

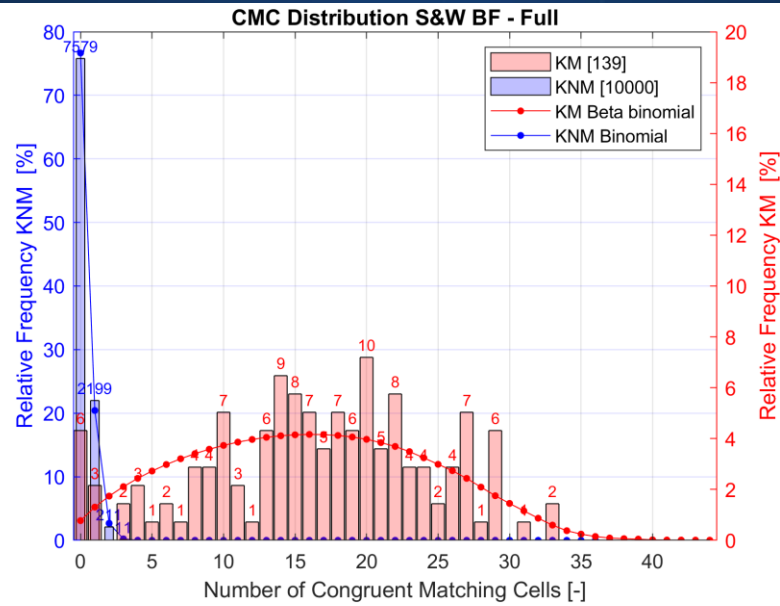


Probability of CMC = 6
given KNM
 $6.81\text{E-}07$

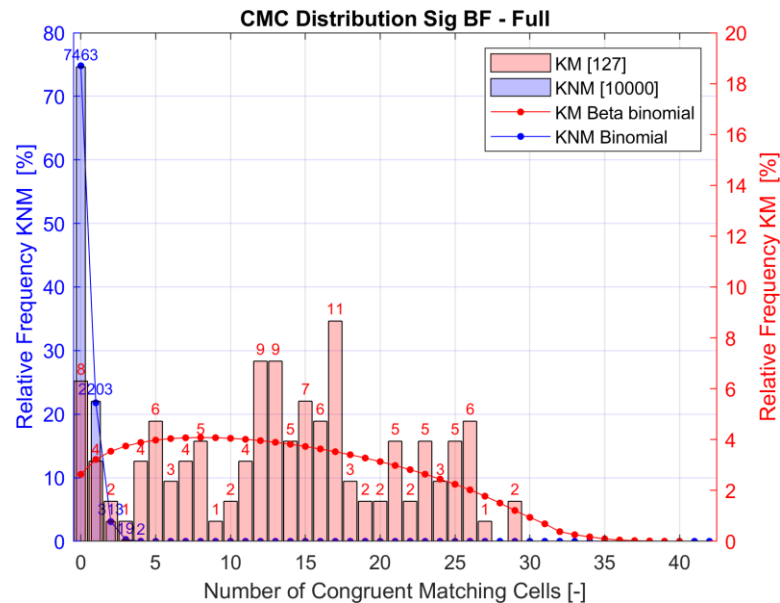


Probability of CMC = 6
given KNM
 $3.03\text{E-}07$

1 in 10 Million

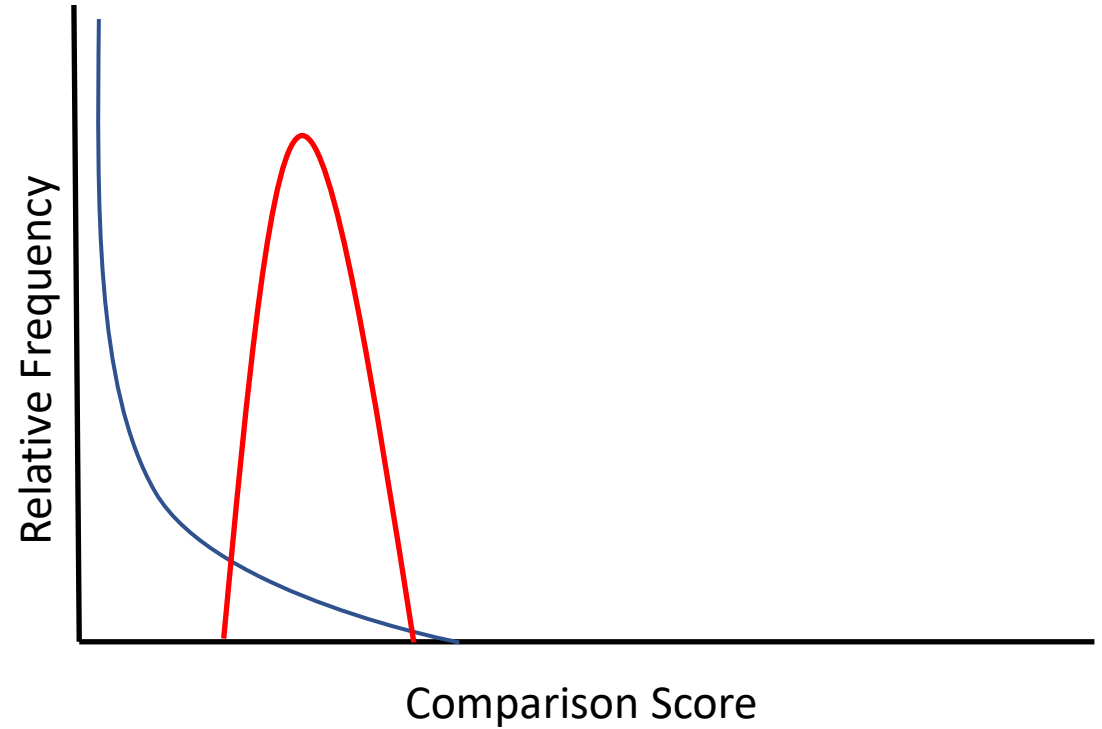
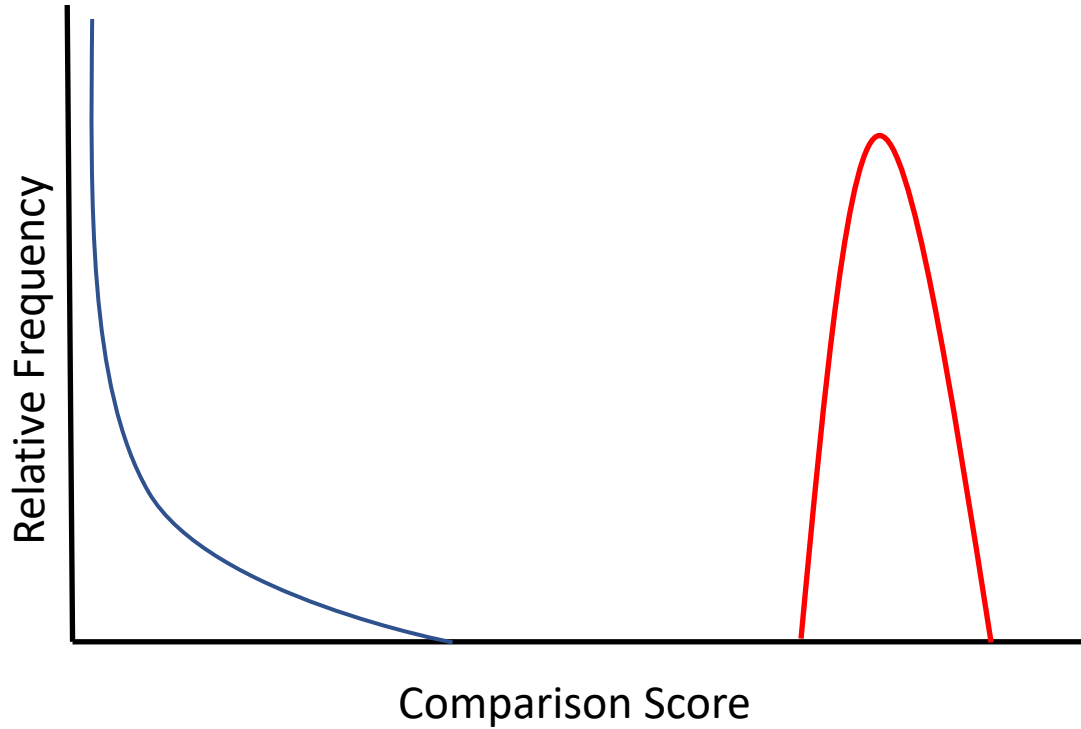


Probability of CMC = 6
given KNM
 $3.03\text{E-}07$



Probability of CMC = 6
given KNM
 $4.44\text{E-}07$

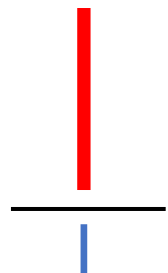
Weigh Both Propositions



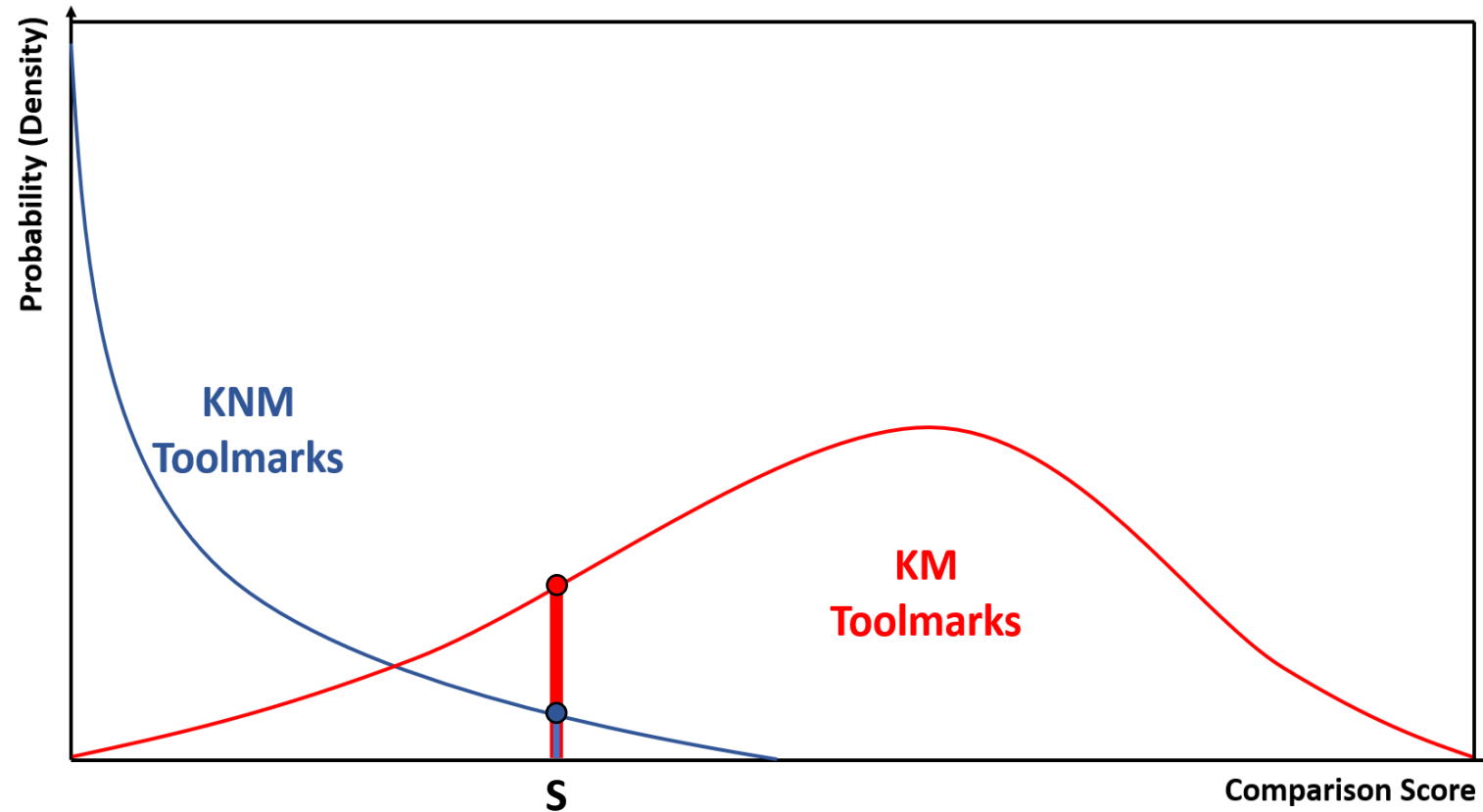
Very different weight of evidence in these two scenarios

Score-based Likelihood Ratios

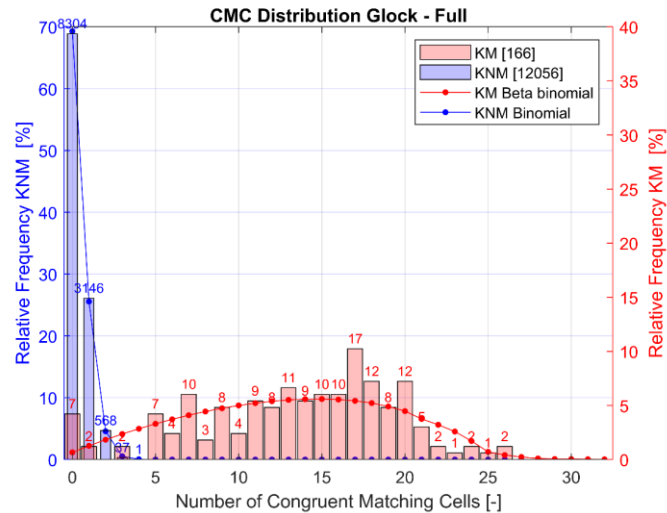
Score-based Likelihood Ratio

$$\text{SLR} = \frac{P(S|\textcolor{red}{KM})}{P(S|\textcolor{blue}{KNM})}$$


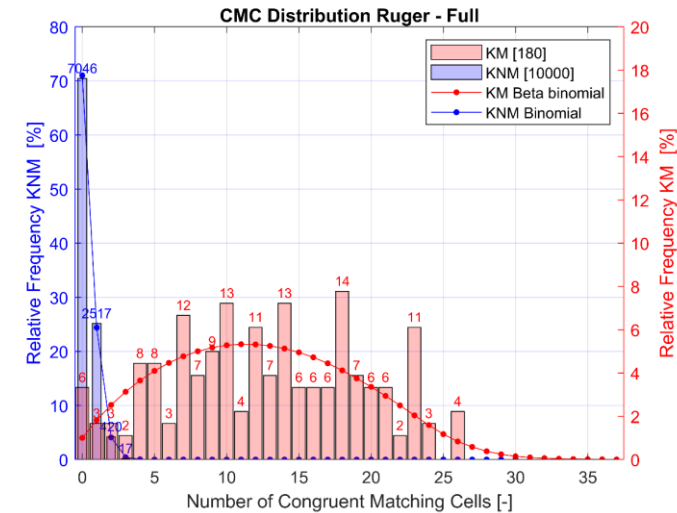
- SLR < 1: Support that this cartridge case did not originate from the suspected firearm
- SLR = 1: Equally likely to observe a score “S” from either the KM and KNM population.
- SLR > 1: Support that this cartridge case originate from the suspected firearm



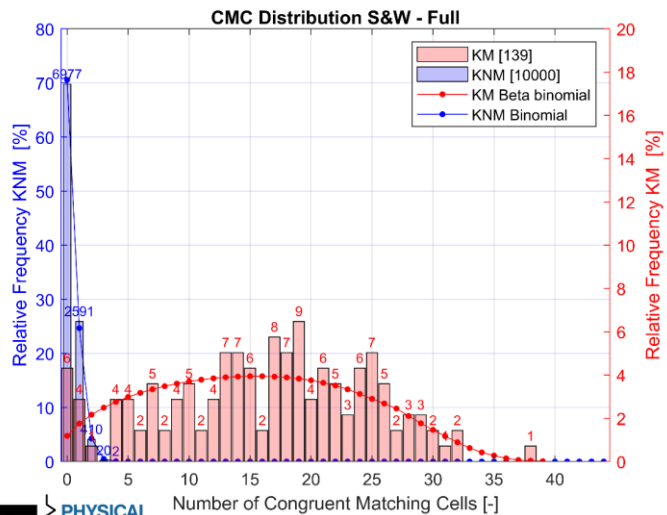
SLRs are not Fixed



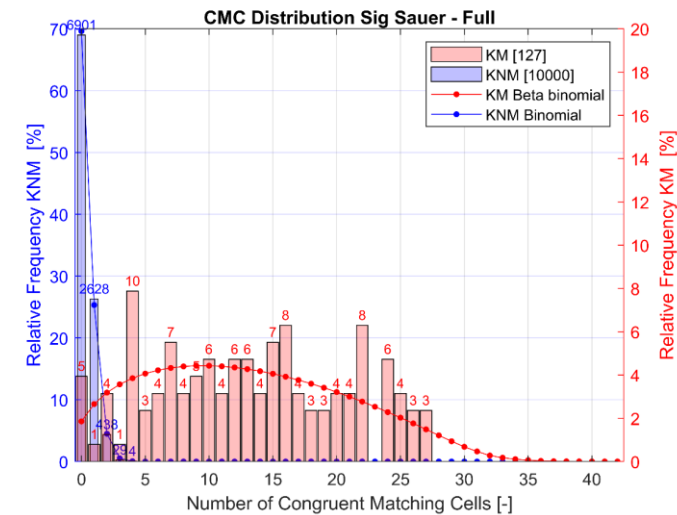
CMC = 6
SLR = 24986



CMC = 6
SLR = 21687

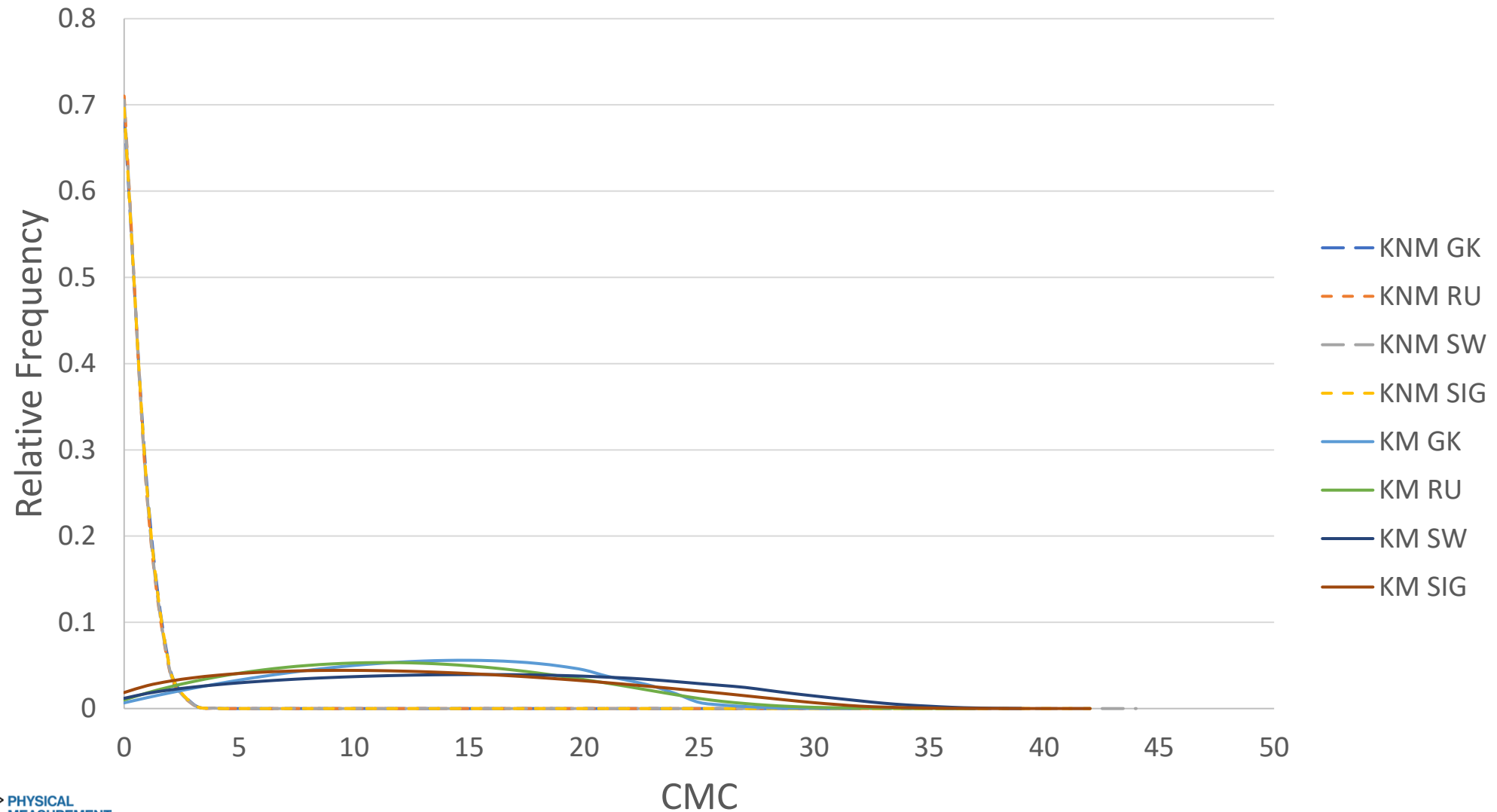


CMC = 6
SLR = 38477

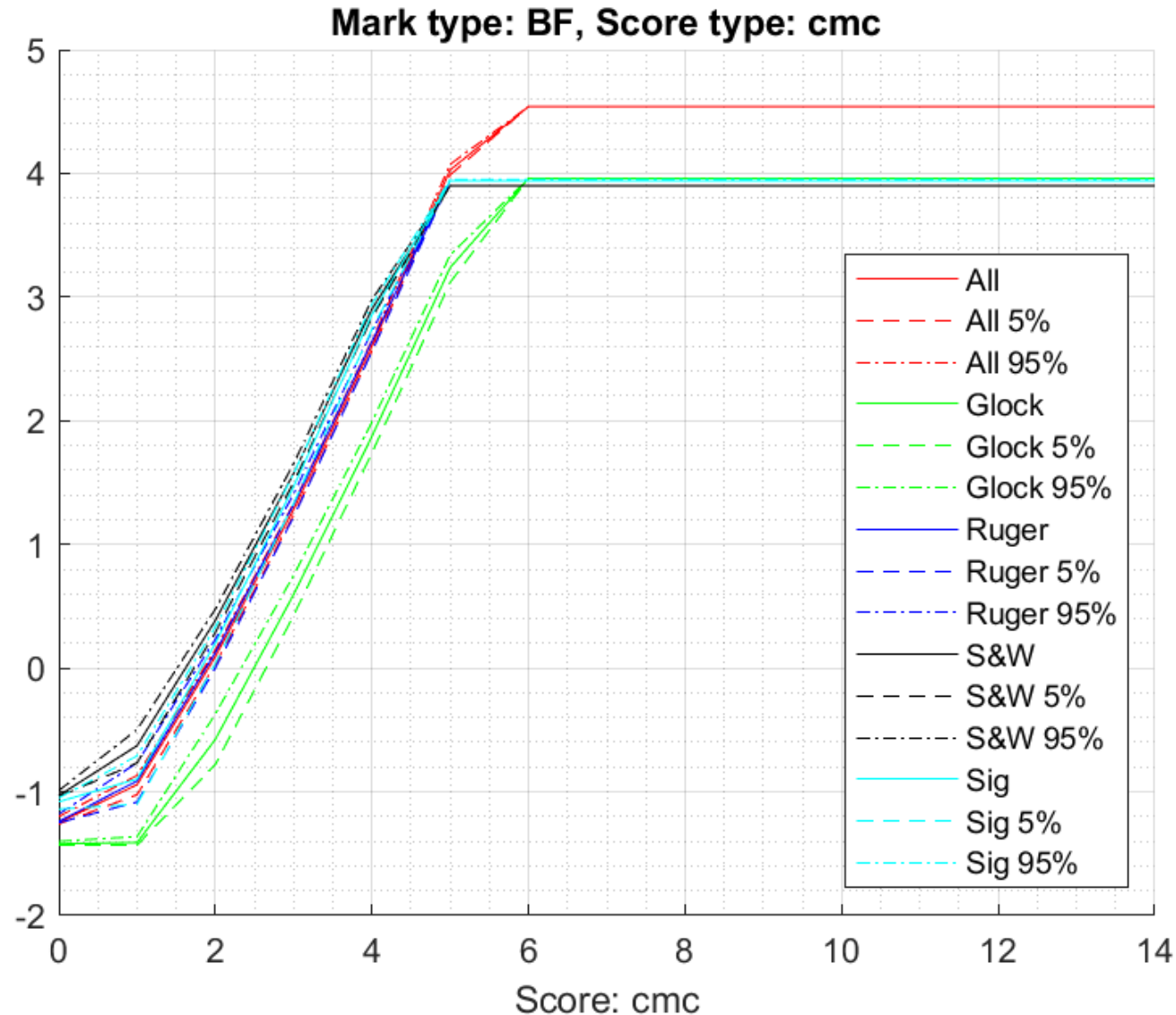


CMC = 6
SLR = 26509

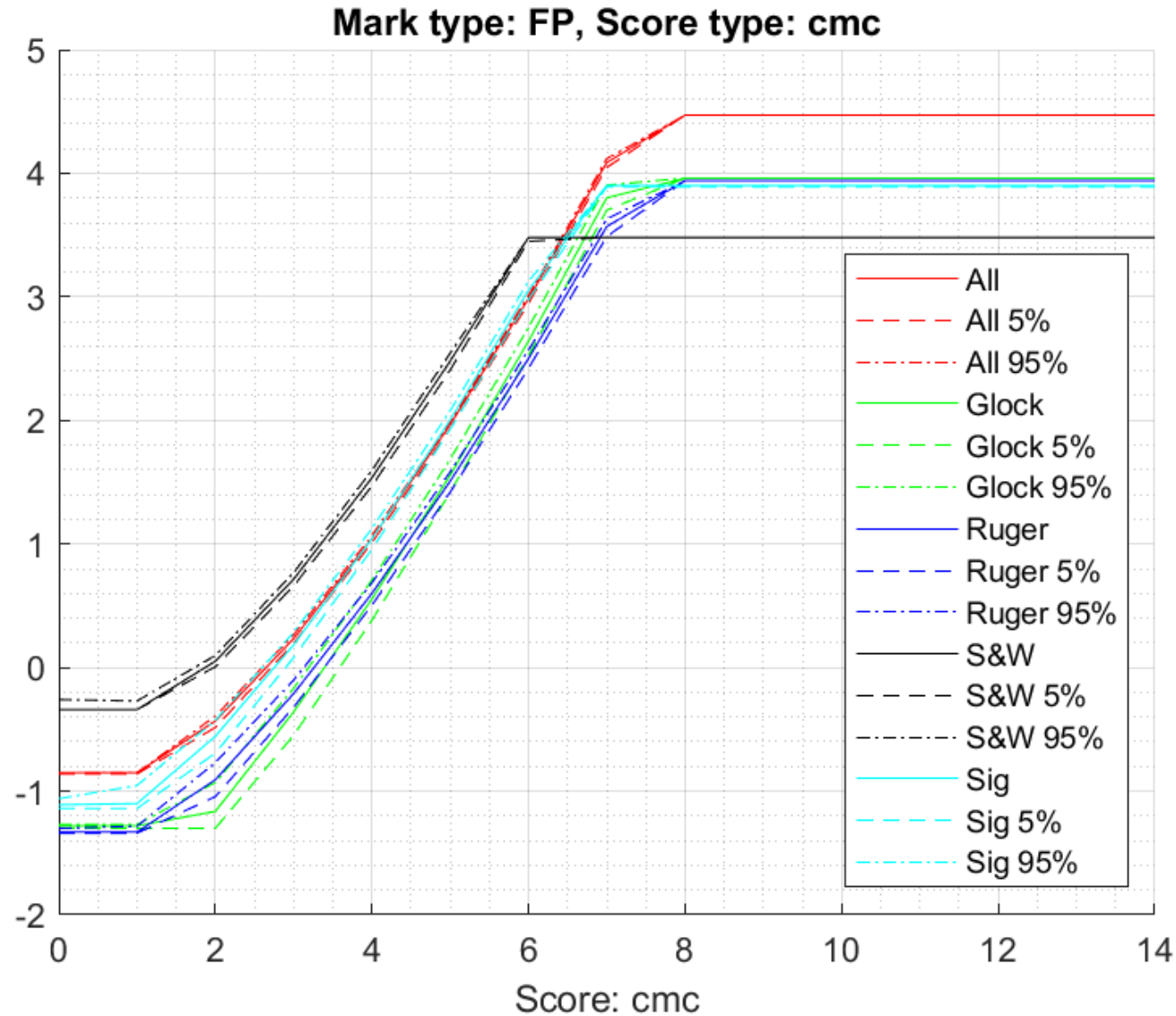
Combine All Four Mfg.



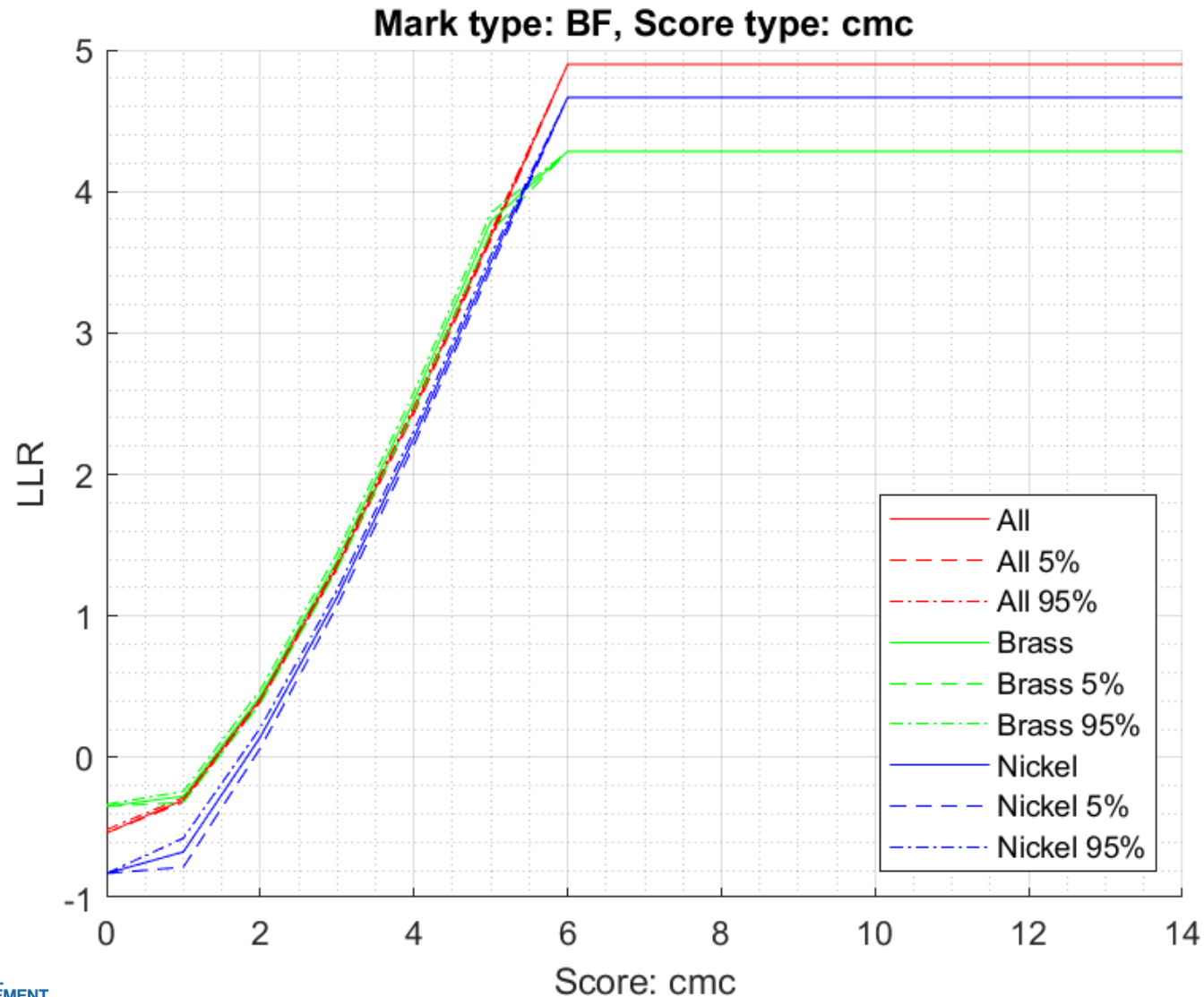
LR with Different Mfg. Distributions



LR with Different Mfg. Distributions



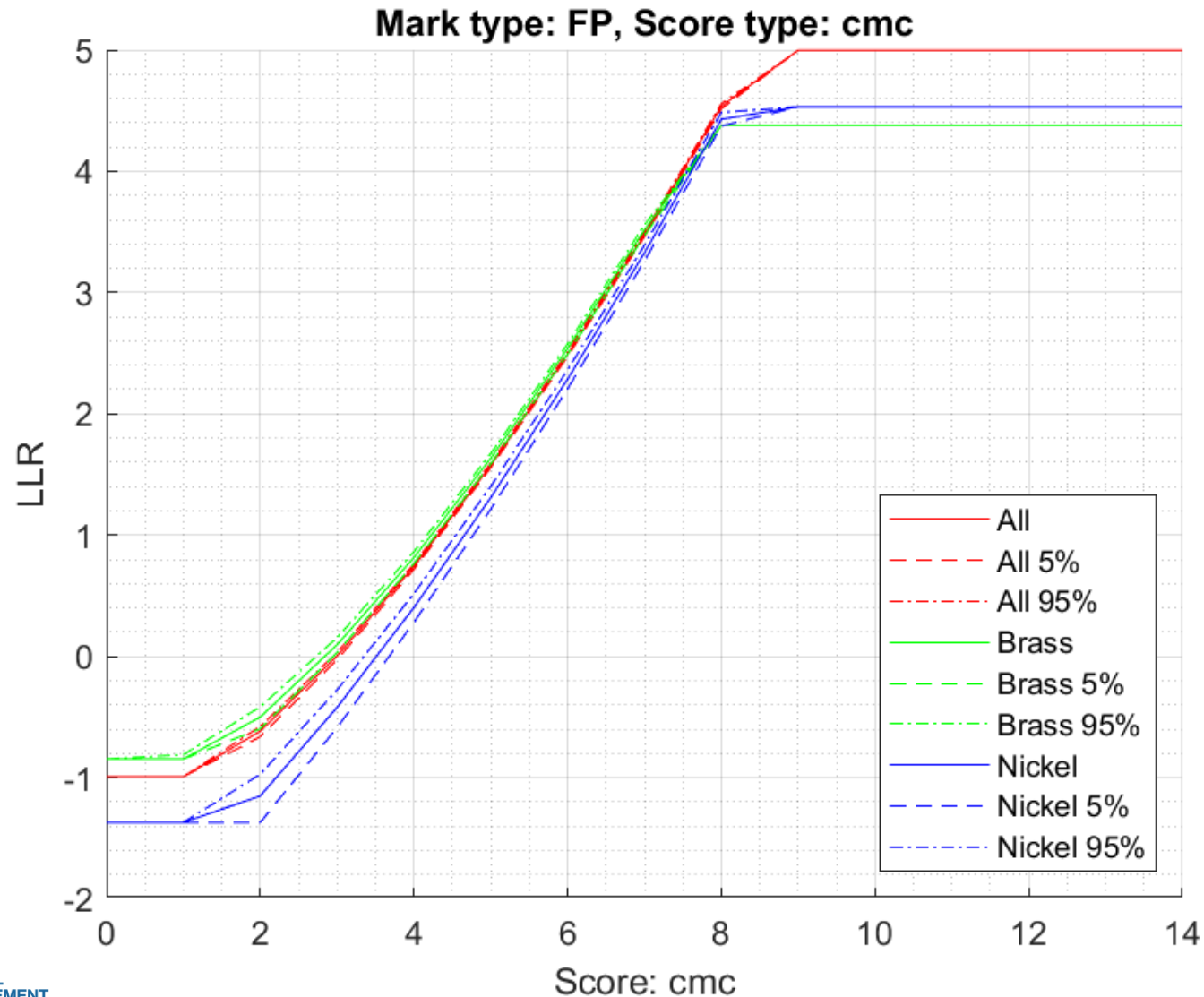
LR with Different Material Types - BF



NFI Glock Database

Analysis conducted by
Dr. Martin Baiker at the
Netherlands Forensics
Institute

LR with Different Material Types - FP



NFI Glock Database

Analysis conducted by
Dr. Martin Baiker at the
Netherlands Forensics
Institute

Discussion

- The CMC algorithm yields repeatably low false positive rates across all populations. This leads to low variability in LR_s across different populations.
- Large reference populations with varying firearm and ammunition class characteristics are required to build the appropriate relevant populations.
- Additional research is required to determine which parameter heavily influence the SLR value.